$$A_B v_B - A_{IB}^T (A_I^{-1} (A_{IB} v_B))$$