$$S_B \equiv A_B - A_{IB}^T A_I^{-1} A_{IB}$$